

ABOUT THE DISTRIBUTION FUNCTION OF THE PRIME NUMBERS

Abstract. In this article we establish a new formula for $\Pi(x) = \sum_{\substack{p \leq x \\ p \text{ prime}}} 1$, the number of primes not greater than x :

$$\Pi(x) = 1 - \sum_{n=1}^{[x]} \left[(-1)^{[\sqrt{n}]+1} \cdot P_n \right] \quad (x \geq 3)$$

where $P_n = \prod_{k=2}^{n-1} \sin \frac{n\pi}{k}$ and $[\]$ denotes integer part.

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