

## On the iterative solution of some decomposable nonlinear operator equations

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### ABSTRACT.

The aim of this note is to extend a recent result concerning the solvability of a nonlinear equation that can be decomposed under the form  $Au = Pu$ , where one of the two operators  $A$  and  $P$  has richer properties than the other one.

**Acknowledgements.** The research was supported by the CEEX Grant No. 2-CEEX-06-11-96/19.09.2006 of the Romanian Ministry of Education and Research. The author also thanks Abdus Salam International Centre for Theoretical Physics (ICTP) in Trieste, Italy, where he was a visiting professor during the writing of this paper.

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Received: 22.09.2006; In revised form: 03.06.2008.; Accepted:  
2000 *Mathematics Subject Classification.* 47H10.

Key words and phrases. *Metric space, operator equation, Picard iteration, solution, convergence theorem.*