Statistical approximation properties of Kantorovich operators based on q-integers

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ABSTRACT.

In this paper we present two new generalizations of Kantorovich operators based on q-calculus. With the help of Bohman-Korovkin type theorem we obtain some statistical approximation properties for these operators. Also, by using the modulus of continuity, the statistical rate of convergence is established.

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