

Computation of bounds for polynomial roots

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ABSTRACT.

We discuss some old and new results on bounds for roots of univariate polynomials, emphasizing on new methods concerning real roots of univariate polynomials with real coefficients. There are presented new methods for computing bounds for positive roots of univariate polynomials. We compare our results with known upper bounds for positive roots.

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