# A note on a difference inequality used in the iterative approximation of fixed points

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# ABSTRACT.

In this note we present a more detailed proof of Lemma 2 in [Liu, L.S., *Ishikawa and Mann iteration process with errors for nonlinear strongly accretive mappings in Banach spaces*, J. Math. Anal. Appl., **194** (1995), 114-125], regarding the global asymptotic stability of the solution of a first order difference inequality.

#### **ACKNOWLEDGEMENTS**

The research was supported by the CEEX Grant 2532 of the Romanian Ministry of Education and Research. The author also thanks Abdus Salam International Centre for Theoretical Physics (ICTP) in Trieste, Italy, where he was a visitor during the writing of this paper.

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Received: 25.02.2009; In revised form: 04.03.2009.; Accepted:

2000 Mathematics Subject Classification. 39A11, 39A99, 40A05.

Key words and phrases. Difference inequality, zero solution, asymptotic stability, Cauchy's lemma.