

On isotopic characterization of central loops

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ABSTRACT.

The representation sets of central loops are investigated and the results obtained are used to construct a finite C - loop. It is shown that for certain types of isotopisms, the central identities are isotopic invariant.

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Received: 8.03.2008; In revised form: 29.09.2008.; Accepted:

2000 Mathematics Subject Classification. 20N05, 08A05.

Key words and phrases. LC-loops, RC-loops, C-loops.