

A new generalization of Euler's constant

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ABSTRACT.

A new generalization of Euler's constant, $c = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{2} + \dots + \frac{1}{n} - \ln n \right)$, this time as a function $\gamma(a, b)$ of two positive real variables, $a \in (0, \infty)$, $b \in \left[0, \frac{1}{2a} \right]$, is given such that, in particular, we have $c = \gamma(1, 0)$.

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