Generalized additive Cauchy equations and their Ulam-Hyers stability

FLORIN BOJOR

ABSTRACT.

In this paper we investigate the Hyers-Ulam-Rassias stability of the following functional equation: $f(a(x) + b(y)) = mf(x) + nf(y)$ in Banach spaces.

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NORTH UNIVERSITY OF BAIA MARE
DEPARTMENT OF MATHEMATICS
AND COMPUTER SCIENCE
VICTORIEI NR. 76
430122 BAIA MARE, ROMANIA
E-mail address: `f_bojor@yahoo.com`