

A possible visual image of the extended monogenous function

LIDIA ELENA KOZMA AND GHEORGHE ARDELEAN

ABSTRACT.

The monogenous functions defined on $R^4 \rightarrow R^4$ were introduced by G.C. Moisil. If we start from monogenous functions on a quaternion, through particularization we only find the monogeneity condition $\frac{\partial w}{\partial \bar{z}} = 0$ for a function $w = f(z) : C \rightarrow C$. In this article the notion of monogeneity is extended from the common complex analysis over to the quaternion functions of two variables, of the following aspect:

$$K = x + iy + ju(x, y) + kv(x, y) = z + jw(x, y) \quad (0.1)$$

and we have visualized the surfaces (S) attached to this quaternion

$$(S) \quad \bar{r} = iy + ju(x, y) + kv(x, y) \quad (0.2)$$

in monogeneity conditions. A few surfaces attached to some elementary monogenous functions have been visualized.

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DEPARTMENT OF MATHEMATICS AND
COMPUTER SCIENCE
NORTH UNIVERSITY OF BAI A MARE
VICTORIEI 76
430122 BAI A MARE, ROMANIA
E-mail address: lidik@ubm.ro
E-mail address: ardelean.g@yahoo.com

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