

On the generalized Stirling formula

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ABSTRACT.

The aim of this paper is to give a numerical construction of the best approximations of the factorial function among the family of approximations introduced by Mortici [Arch. Math. (Basel) 93 (2009), No. 1, 37-45].

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