

A weighted inequality involving the sides of a triangle

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ABSTRACT.

A new weighted inequality involving the sides of a triangle is proved by applying the method of the Difference Substitution, and, as an application, a geometric inequality involving an interior point of the triangle is derived. Finally, two related conjectures which are checked by computer are put forward.

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