

A simple proof of Gautschi-Kershaw inequality

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ABSTRACT.

The aim of this paper is to give a simple proof of Gautschi-Kershaw inequality.

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