## Hardy-Hilbert integral inequality with weights

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## ABSTRACT.

We study a Hardy-Hilbert integral inequality with weights by introducing a weight function of the form  $x_r^2 - 1$  (with r > 1), and prove the constant factor to be the best possible, and give an extension of the Hilbert integral inequality, and then consider some equivalent forms.

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