

Some remarks on the Krasnoselskij iterative method

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ABSTRACT.

In this paper we deal with some convergence results regarding the Krasnoselskij iterative scheme. New proofs for known results like Proposition 3.2 or Theorem 1.1 as well as new results like Proposition 3.4 or Proposition 4.5, are presented.

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