

## About the implementation and some applications of the FIXPOINT software minipackage

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### ABSTRACT.

The main aim of this note is to briefly present the implementation, main features and some current and potential applications of the software minipackage FIXPOINT, designed and implemented by the first author and used by the second author in solving some concrete problems.

**Acknowledgements.** The second author's research was supported by the Grants PN-II-RU-TE-2011-3-239 and PN-II-ID-PCE-2011-3-0087 of the Romanian Ministry of Education and Research.

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Received: 25.05.2014; In revised form: 26.05.2014; Accepted: 02.06.2014

2010 Mathematics Subject Classification. 47H10, 47J25, 49M15, 49M30.

Key words and phrases. Fixed point, piecewise linear, homotopy, algorithm, implementation, optimization problem, Schwefel's function.

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