Properties and inequalities for the $h$- and $(h, m)$-logarithmically convex functions

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Abstract. In the paper, the authors introduce definitions of $h$-logarithmically convex functions and $(h, m)$-logarithmically convex functions respectively, discuss some properties of these kinds of functions, and establish some integral inequalities for these kinds of functions.

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