

The Voronovskaja-type formula for the Bleimann, Butzer and Hahn operators

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ABSTRACT.

We present a short and simple proof to the Voronovskaja-type formula for the Bleimann, Butzer and Hahn operators. The proof is essentially based on the relationship between the Bleimann, Butzer and Hahn operators and the Stancu operators.

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