

## The recurrence theorem of Frenet formulae

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### ABSTRACT.

In this paper we generalize Frenet trihedron and we provide some other classes of trihedrons, called Frenet trihedrons of order  $n$ ,  $n \geq 1$ . Moreover we prove that those trihedrons can be defined recurrently and we emphasize their role in the study of the generalized helices of order  $n$ . As practical applications we present the influence of the recurrence theorem in some interdisciplinary domains like physics, chemistry and biology.

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