

The crossing numbers of products of paths with 7–vertex trees

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ABSTRACT.

The crossing numbers of Cartesian products of paths with all graphs of order at most five are given. The crossing numbers of Cartesian products of paths with several graphs on six vertices are known. We extend these results by giving the exact values or upper bound of crossing numbers of Cartesian products $G \square P_n$ for every tree G on seven vertices.

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