

Common fixed point and best approximation results for subcompatible mappings in hyperbolic ordered metric spaces

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ABSTRACT.

In the present paper we establish a common fixed point theorem and apply it to find new best approximation results for ordered subcompatible mappings in the hyperbolic ordered metric space. Our results unify, generalize and complement various known results.

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