A hybrid iterative method without extrapolating step for solving mixed equilibrium problem

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ABSTRACT.

In this paper, we introduce a hybrid iterative method without extrapolating step to approximate a solution of mixed equilibrium problem in real Hilbert space. We prove a strong convergence theorem for the sequences generated by the proposed iterative algorithm. The result presented in this paper is the extension and generalization of the previously known results in this area.

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