Kannan contractions and strongly demicontractive mappings

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Abstract.

Inclusion relations between strongly demicontractive mappings, quasi (L, m)-contractions, and Kannan contractions are established. As corollaries, *T*-stability and strong convergence of Picard and Mann iterations for strongly demicontractive mappings are obtained.

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