

## Some inequalities for geometrically-arithmetically $h$ -convex functions

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### ABSTRACT.

In this paper, we consider a class of geometrically convex function which is called geometrically-arithmetically  $h$ -convex function. Some inequalities of Hermite-Hadamard type for geometrically-arithmetically  $h$ -convex functions are derived. Several special cases are discussed.

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