

Some conjugate WP-Bailey pairs and transformation formulas for q -series

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ABSTRACT.

In this paper, the authors prove several theorems involving q -series identities by applying a certain family of conjugate WP-Bailey pairs. Making use of these theorems in conjunction with some WP-Bailey pairs, various transformation formulas for q -series are also established.

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